

Year 9 Strand 4

Topic/Skill	Definition/Tips	Example
Solving Simultaneous Equations (by Elimination)	<ol style="list-style-type: none"> 1. Balance the coefficients of one of the variables. 2. Eliminate this variable by adding or subtracting the equations (Same Sign Subtract, Different Sign Add) 3. Solve the linear equation you get using the other variable. 4. Substitute the value you found back into one of the previous equations. 5. Solve the equation you get. 6. Check that the two values you get satisfy both of the original equations. 	$5x + 2y = 9$ $10x + 3y = 16$ <p>Multiply the first equation by 2.</p> $10x + 4y = 18$ $10x + 3y = 16$ <p>Same Sign Subtract (+10x on both)</p> $y = 2$ <p>Substitute $y = 2$ in to equation.</p> $5x + 2 \times 2 = 9$ $x = 1$ <p>Solution: $x = 1, y = 2$</p>
Solving Simultaneous Equations (by Substitution)	<ol style="list-style-type: none"> 1. Rearrange one of the equations into the form $y = \dots$ or $x = \dots$ 2. Substitute the right-hand side of the rearranged equation into the other equation. 3. Expand and solve this equation. 4. Substitute the value into the $y = \dots$ or $x = \dots$ equation. 5. Check that the two values you get satisfy both of the original equations. 	$y - 2x = 3$ $3x + 4y = 1$ <p>Rearrange: $y - 2x = 3 \rightarrow y = 2x + 3$</p> <p>Substitute: $3x + 4(2x + 3) = 1$</p> <p>Solve: $3x + 8x + 12 = 1$</p> $11x = -11$ $x = -1$ <p>Substitute: $y = 2 \times -1 + 3$</p> $y = 1$ <p>Solution: $x = -1, y = 1$</p>
Quadratic Graph	<p>A 'U-shaped' curve called a parabola. The equation is of the form $y = ax^2 + bx + c$, where a, b and c are numbers, $a \neq 0$. If $a < 0$, the parabola is upside down.</p>	
Roots of a Quadratic	<p>A root is a solution.</p> <p>The roots of a quadratic are the x-intercepts of the quadratic graph.</p>	
Probability	<p>The likelihood/chance of something happening.</p> <p>Is expressed as a number between 0 (impossible) and 1 (certain).</p> <p>Can be expressed as a fraction, decimal, percentage or in words (likely, unlikely, even chance etc.)</p>	

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Probability Notation	P(A) refers to the probability that event A will occur.	P(Red Queen) refers to the probability of picking a Red Queen from a pack of cards.
Theoretical Probability	$\frac{\text{Number of Favourable Outcomes}}{\text{Total Number of Possible Outcomes}}$	Probability of rolling a 4 on a fair 6-sided die = $\frac{1}{6}$.
Relative Frequency	$\frac{\text{Number of Successful Trials}}{\text{Total Number of Trials}}$	A coin is flipped 50 times and lands on Tails 29 times. The relative frequency of getting Tails = $\frac{29}{50}$.
Expected Outcomes	To find the number of expected outcomes, multiply the probability by the number of trials.	The probability that a football team wins is 0.2 How many games would you expect them to win out of 40? $0.2 \times 40 = 8 \text{ games}$
Tree Diagrams	Tree diagrams show all the possible outcomes of an event and calculate their probabilities. All branches must add up to 1 when adding downwards. This is because the probability of something not happening is 1 minus the probability that it does happen. Multiply going across a tree diagram. Add going down a tree diagram.	
Independent Events	The outcome of a previous event does not influence/affect the outcome of a second event.	An example of independent events could be <u>replacing</u> a counter in a bag after picking it.
Dependent Events	The outcome of a previous event does influence/affect the outcome of a second event.	An example of dependent events could be not replacing a counter in a bag after picking it. 'Without replacement'
Venn Diagrams	A Venn Diagram shows the relationship between a group of different things and how they overlap. You may be asked to shade Venn Diagrams as shown below and to the right.	
Venn Diagram Notation	∈ means ' element of a set ' (a value in the set) { } means the collection of values in the set.	Set A is the even numbers less than 10. $A = \{2, 4, 6, 8\}$

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	ξ means the 'universal set' (all the values to consider in the question)	Set B is the prime numbers less than 10. $B = \{2, 3, 5, 7\}$
	A' means 'not in set A' (called complement)	$A \cup B = \{2, 3, 4, 5, 6, 7, 8\}$
	A \cup B means 'A or B or both' (called Union)	$A \cap B = \{2\}$
	A \cap B means 'A and B (called Intersection)	